Concentration of Solar Energy Using Optical Systems Designed from a Set of Conical Rings

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1. Introduction

Different types of optic systems have been designed, manufactured, and used to concentrate energy, be it solar or otherwise. To mention just a few, we have for example, 1) the design and manufacture of a non-imaging Fresnel lens prototype for use in a solar collector of medium concentration (Leutz et al., 2000). This collector was evaluated in terms of the optical concentration ratio of its lens and the flux distribution on the absorber; 2) the design and manufacture of a low-frequency Fresnel mirror for a fluorescence detector (Díaz-Anzures et al., 2004), in which the Fresnel mirror was formed from a set of concentric spherical rings; 3) the design of mirrors from a set of spherical rings to generate an angular zone of energy concentration one order of magnitude smaller in comparison to the spot size generated with a spherical mirror (González-García et al., 2009), and 4) the optical design of a highly radiative solar flux furnace for Mexico (Riveros-Rosas et al., 2010) which consisted of an arrangement of 409 first surface spherical facets with a hexagonal shape. The configuration of this design was chosen because of its maximum peak concentration and also for economical reasons.

In the case of concentrator systems which involve polished elements such as lenses and/or mirrors, polishing techniques and optical tests are required for their manufacture. In order to reduce time and costs in the manufacture of solid mirrors designed by the concept of concentric spherical rings (a design method proposed more as an alternative in the design of energy concentrating lens and mirrors (González-García et al., 2009)), a classical polishing method was proposed using petal tools designed with Genetic Algorithms (González-García, et al., 2006) and with linear programming, (Santiago-Alvarado, et al., 2007). These lenses or mirrors can also be polished using different-shaped oscillating tools (Leal-Cabrera, et al., 2009). One alternative for testing the quality of polished surfaces is the application of the Ronchi Test (Cornejo-Rodríguez, 2007), which is an inexpensive test and easy to apply. Based on the ronchigram of the surface being tested, and applying Malacara's formula, cubic splines, and Genetic Algorithms, surface errors can be quantified (Cordero-Dávila & González-García, 2010; Cordero-Dávila, et al., 2011).

According to the analysis of the influence of the amount of circumsolar radiation in function of the acceptance angle of the absorber (Buie & Monger, 2004), the results showed that as the CSR of the sunshape increases, the size of the absorber must also increase to accommodate a similar amount of energy, that is, the size of the image increases. For this reason, a previous study proposed the design and manufacture of a mirror that would generate a desired angular size of the concentration of energy (González-García, et al., 2009). One hundred spherical rings, whose optimum curvature radius values were calculated with Genetic Algorithms (GA), were employed in the modeling process of the mirror (see Fig. 1). Using the Full Width at Half Maximum criterion (FWHM), the size of the sun-image obtained with this mirror was 16.82 mm, as shown in Fig. 2.

Fig. 1. Mirror modelled from a set of concentric spherical rings.

Fig. 2. Sun image generated with the mirror designed from a set of concentric spherical rings: (a) spot diagram and (b) graph of irradiance distribution.

The content of this chapter focuses on the description of a method for designing mirrors that would generate a desired angular size of a point source placed at infinity. Based on the simulation of the mirror by means of the ZEMAX optic design program (ZEMAX, Software For Optical System Design, 2008), the simulated mirror would later generate the corresponding image of the sun. The method for designing mirrors will be based on the above mentioned study of the design of mirrors from a set of concentric spherical rings. In order to be able to generalize the method not only spherical surface rings but also rings with any type of conic surface will be taken into account, that is, rings with any conic surface. One implication of this is that the angular size of the image (found during the optimization

stage using GA) will now be in function of the conic constant, be it through a predetermined value, or by considering it as a variable to be optimized together with the paraxial curvature radius of each ring. The sun images generated by four mirrors designed from rings whose surfaces have a determined value of the conic constant for each design will be simulated.

2. Design and optimization

In line with the procedure for designing a mirror from set of concentric spherical rings which reduce by one order of magnitude the size of an image of a point source placed at infinity, this section presents the design of four mirrors from concentric rings with conic profile whose conic constant for each case are: zero, (original design (González-García, et al., 2009) taken as a comparison), -1 (parabolic rings), -0.5 (rings with elliptical profile), and -1.6279, whose value was calculated with the GA together with the corresponding curvature radii.

2.1 Design of energy concentrating mirrors

Just like the original design (González-García, et al., 2009), these designs of the mirrors are also intended to reduce, by one order of magnitude the angular size of the image generated by a spherical mirror whose parameters are 1,500 mm in diameter, a curvature radius of 4,000 mm, and a focal distance of 2,000 mm. generating a disc of least confusion of 0.20966 degrees at a distance of -1,973.0 mm

The design procedure, considering the GA optimization method is expressed through the following steps:

1. 100 rings are used to model the shape of the mirror surface (from a reference sphere with a curvature radius of 3,900 mm, considered for the manufacture stage, by means of petal tool polishing (González-García, et al., 2006)). This involves calculating 100 curvature radii that are the variables to be considered in the optimization.
2. In order to reduce the number of variables to be optimized a recurrence formula was employed to reduce the number of variables from 100 to 20, expressed as

$$r_{i+1} = r_i + \Delta r_j \quad (1)$$

where r_i ($i=1,\dots,100$) are the curvature radii of each one of the rings and Δr_j ($j=1,\dots,20$) are the increments of the curvature radii, which would be the variables to be optimized by the GA. These increments are defined by the following equation

$$\Delta r_j = \begin{bmatrix} m_1 & \text{if} & 1 \leq i \leq 5 \\ m_2 & \text{if} & 6 \leq i \leq 10 \\ \vdots & & \\ m_{20} & \text{if} & 96 \leq i \leq 100 \end{bmatrix} \quad (2)$$

3. The fitness function is established as the error square of the differences between the simulated angular size (sas) and the desired angular size (das)

$$\text{Fitness Function} = S^2 = (\text{sas} - \text{das})^2 \quad (3)$$

4. For the first three mirror designs the conic constant of the rings are considered constant whereas for the last design the conic constant is considered as just one more variable to be calculated by the GA, thereby establishing a more general method of design.

Once the design process of the energy concentrating mirrors has been established, the next process is the optimization of the twenty increments of the curvature radii defined by equations 1 and 2. The following is a description of the GA applied to optimize the design of the mirrors.

2.2 Genetic algorithm applied

The optimization method applied to calculate the optimum designs of the mirrors is a GA programmed in FORTRAN for LINUX. It has been used in classical surface polishing (González-García, et al., 2006), in the field of optical testing using Ronchi tests (Cordero-Dávila, et al., 2011), and in optical design (González-García, et al., 2009). The content of this chapter is one more example of this latter application. The stages of the GA applied are briefly described as follows:

A. Generation of the initial population

In this stage an initial random population of 240 individuals was created for each one of the twenty increments of the curvature radii. Hence, the total number of individuals or values randomly generated in this stage is the product 240X20. Within the area of programming 240 chromosomes were programmed, each one with a longitude of 320 genes. Each one of these chromosomes is divided into 20 chromosomes more (of 16 genes), and each one is used to calculate the value corresponding to each one of the increments of the curvature radii. Fig. 3 shows part of the programming corresponding to this stage.

```

INTEGER lcromosoma, tpoblacion,maxgeneraciones
PARAMETER (lcromosoma=320, tpoblacion=240 ,maxgeneraciones=160)

nvar = 20

do ii=1,tpoblacion
  do jj=1, lcromosoma

    CALL RA(srand)
    a = rand(srand)
    CALL flips(0.5,a,gene)
    pob(ii,jj) = gene

  enddo
enddo

```

Fig. 3. Programming implemented for the generation of the initial population.

B. Evaluation stage

Once the initial population has been created, the evaluation stage is performed to determine, by means of the fitness function, Eq. (3), which chromosomes (of 16 genes) are the best values assigned to the increments of the curvature radii, with which Eq. (3) generates a minimum value. This stage was programmed as a subroutine within which the subroutine of ray tracing is found, and with which the simulated angular size is calculated.

C. The selection stage

The next stage in the GA is the selection stage in which the best values of the curvature radii increments are selected by means of the corresponding chromosomes graded as such in the evaluation stage. The selection process employed the tournament technique (González-García, et al., 2009), which consists of randomly taking a certain number of individuals from the population, called tournament size; from this, one of the individuals of the set is chosen for the next generation. The process is repeated as many times as there are individuals in the population, in the present case 240 times. Fig. 4(a) shows the subroutine corresponding to this stage.

```

SUBROUTINE SelecTorneo(tpoblacion,FSE,croele)
integer nm, st, stf, srnd, tpoblacion, ab(10)
integer ab1, ab2, croele(tpoblacion), stcroele
REAL a, FSE(tpoblacion), ps_st
nm = 0
ps_st = 0.95
do st=1, tpoblacion
  nm = nm+1
  do stf=1, 2
    CALL RAV2(stf, nm, srnd)
    a = rand(srnd)
    ab(stf) = int(float(tpoblacion)*a)
  enddo
  ab1 = ab(1)
  ab2 = ab(2)
  CALL RAV1(nm, srnd)
  a = rand(srnd)
  if (FSE(ab1).gt.FSE(ab2)) then
    stcroele1 = ab1
    stcroele2 = ab2
  else
    stcroele1 = ab2
    stcroele2 = ab1
  endif
  if (a.le.ps_st) then
    croele(st) = stcroele1
  else
    croele(st) = stcroele2
  endif
enddo
END

```

(a)

```

CALL aleatoriocruza(lcromosoma, nvar, ii, acru2)
jcruza = acru2
ii = nm+1
CALL aleatoriocruza(lcromosoma, nvar, ii, acru2)
jcruza1 = acru2
if (jcruza1.lt.jcruza) then
  band = jcruza
  jcruza = jcruza1
  jcruza1 = band
else
  endif
do jcru=1, jcruza
  hijo1(icru, jcru) = pobp1(conyugue2, jcru)
  hijo2(icru, jcru) = pobp1(conyugue1, jcru)
enddo
do jcru=jcruza+1, jcruza1
  hijo1(icru, jcru) = pobp1(conyugue1, jcru)
  hijo2(icru, jcru) = pobp1(conyugue2, jcru)
enddo
if (jcruza1.ne.lcromosoma) then
  do jcru=jcruza1+1, lcromosoma
    hijo1(icru, jcru) = pobp1(conyugue2, jcru)
    hijo2(icru, jcru) = pobp1(conyugue1, jcru)
  enddo
else
  endif
do jei=1, lcromosoma
  pobpn(conc, jei) = hijo1(icru, jei)
  pobpn(conc+1, jei) = hijo2(icru, jei)
enddo

```

(b)

```

pm = 1.0 / tpoblacion
do imuta=1, tpoblacion
  do jmuta=1, lcromosoma
    mnta = mnta + 1
    nm = mnta
    CALL RAV1(nm, srnd)
    a = rand(srnd)
    if (a.lt.pm) then
      if (pobp1(imuta, jmuta).eq.1) then
        pobp1(imuta, jmuta) = 0
      else
        if (pobp1(imuta, jmuta).eq.0) then
          pobp1(imuta, jmuta) = 1
        else
          endif
        endif
      else
        endif
    endif
  enddo
enddo

```

(c)

Fig. 4. Parts of the program implemented for Genetic Algorithm in FORTRAN corresponding to the stages of (a) selection, b) crossing, and c) mutation.

D. Crossing stage

The next stage to be applied is the crossing stage which involves combining two values of each increment of the curvature radius selected from the previous stage with a view to creating better values of these increments, in other words, values which would make the fitness function generate values close to zero. The crossing technique defined was implemented at two points. Fig. 4(b) shows part of the programming of this implementation.

E. Mutation stage

The mutation technique implemented was one in which all the genes of each chromosome of the population have the same probability of being mutated. The mutation probability value

was the inverse of the size of the population. Fig. 4(c) shows the programming corresponding to this stage.

Once the mutation stage has been completed, the evaluation stage is applied once more to determine which members are the best solutions. The whole process is repeated all over again (application of the selection, crossover and mutation stages) to generate populations with better solutions. Each repetition of the process is known as a generation, and as generations come and go, the solutions generated get closer and closer to the optimum solution to the problem. In our application, a population of 240 members was used from a search throughout 160 generations, see Fig. 3.

2.3 Results obtained from optimization

The results obtained from GA correspond to the design of 4 mirrors to reduce by one order of magnitude the angular size of the spherical mirror considering as object a point source located at infinity. As previously mentioned, in each design the concentric rings which model the surface of the mirror now have a conic surface profile.

Fig. 5 shows the evaluation graphs of the GA by means of the fitness function against the number of generations corresponding to each one of mirrors designed with different conic constants. Table 1 shows the energy distribution data generated by each mirror.

Parameter	Type of conical ring used: Spherical	Type of conical ring used: Parabolic	Type of conical ring used: Elliptical	Type of conical ring used: Optimized conic constant
Conic constant	0	-1	-0.5	-1.6279
Image position (mm)	-1973	-1973	-1973	-1973
Total spot size (mm)	0.8405	0.7399	0.7456	0.8449
Geometrical spot size (mm)	0.2370	0.1996	0.1907	0.2105
Geometrical rms X/Y spot size (mm)	0.1676	0.1411	0.1349	0.1488
Angular spot size (°)	0.0244	0.0215	0.0217	0.0240

Table 1. Data of energy distribution of the four designed mirrors.

Fig. 6 shows the energy distribution generated by each mirror, while Fig. 7 shows the corresponding values of the optimal curvature radii found with GA by means of increments of the curvature radii.

Based on the results obtained from the optimization of the designed mirrors, one can conclude that it is possible to design mirrors which concentrate energy in a smaller area reducing the angular size of the concentration, based on the concept of concentric rings which have a conic type surface, establishing in the design process a conic constant with a specific value or considering it as one more variable to be calculated with the GA.

Fig. 5. Graphs of the fitness function as a function of the number of generations produced by the GA for the design of mirrors by means of concentric rings with conic constants of a) 0, b) -1, c) -0.5, and d) -1.6279

Fig. 6. Distribution of energy generated by the mirrors designed with conic constants of a) 0, b) -1, c) -0.5 and d) -1.6279.

Fig. 7. Graphs of the optimized curvature radii of the concentric rings which model the 4 mirrors designed with conic constants of a) 0, b) -1, c) -0.5 and d) -1.6279.

3. Simulations done with ZEMAX. Images generated from the sun source

To consider the sun as an object in the mirrors designed in the previous section, these designs were simulated using the commercial optical design program in version EE of ZEMAX. In order to verify the results obtained of the angular size from each mirror in the optimization stage, see Table 1, the simulations were first done considering as object a point source placed at infinity. Afterwards, the point source was replaced by the sun source in order to generate the corresponding images.

3.1 Simulations done using a point source

To do the simulations of the designed mirrors from the concentric rings, the Non-Sequential Mode option was selected in the ZEMAX program. This mode is primarily used for non-imaging applications and its main analysis feature is the ray-trace detector which gives spatial and angular data on incoherent or coherent rays. Fig. 8 shows the statement of the point source, while Fig. 9 shows the statement of some of the curvature radii of the concentric rings through their corresponding aperture and conic constant data. Fig. 10 shows the diagram of rays in the mirror, while Fig. 11 shows the mirror as seen from the front.

Fig. 8. Statement of the point source in ZEMAX used in the simulation of the designed mirrors.

Non-Sequential Component Editor									
Object Type	Material	Radius	Chord	Max Apert	Min Apert	Par. 3 (mm)	Par. 4 (mm)	Par. 5 (mm)	Par. 6 (mm)
1 Standard Sur.	IR1000	-3900.000000	0.000000	0.000000	0.000000				
2 Standard Sur.	IR1000	-3900.806380	0.000000	15.000000	7.500000				
3 Standard Sur.	IR1000	-3908.616790	0.000000	22.000000	11.000000				
4 Standard Sur.	IR1000	-3906.413130	0.000000	30.000000	15.000000				
5 Standard Sur.	IR1000	-3913.233000	0.000000	37.000000	18.500000				
6 Standard Sur.	IR1000	-3914.724340	0.000000	41.000000	20.500000				
7 Standard Sur.	IR1000	-3917.029420	0.000000	42.000000	21.000000				
8 Standard Sur.	IR1000	-3920.127990	0.000000	40.000000	20.000000				
9 Standard Sur.	IR1000	-3920.127990	0.000000	40.000000	20.000000				
10 Standard Sur.	IR1000	-3920.127990	0.000000	40.000000	20.000000				
11 Standard Sur.	IR1000	-3920.127990	0.000000	40.000000	20.000000				
12 Standard Sur.	IR1000	-3920.127990	0.000000	40.000000	20.000000				
13 Standard Sur.	IR1000	-3920.127990	0.000000	40.000000	20.000000				
14 Standard Sur.	IR1000	-3920.127990	0.000000	40.000000	20.000000				

Non-Sequential Component Editor									
Object Type	Material	Radius	Chord	Max Apert	Min Apert	Par. 3 (mm)	Par. 4 (mm)	Par. 5 (mm)	Par. 6 (mm)
51 Standard Sur.	IR1000	-4003.162600	0.000000	667.000000	660.000000				
52 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
53 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
54 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
55 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
56 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
57 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
58 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
59 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
60 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
61 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
62 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
63 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
64 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
65 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
66 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
67 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
68 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
69 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
70 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
71 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
72 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
73 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
74 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
75 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
76 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
77 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
78 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
79 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
80 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
81 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
82 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
83 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
84 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
85 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
86 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
87 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
88 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
89 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
90 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
91 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
92 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
93 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
94 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
95 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
96 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
97 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
98 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
99 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
100 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
101 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				
102 Standard Sur.	IR1000	-4004.000000	0.000000	670.000000	665.000000				

Fig. 9. Statement of the concentric rings in ZEMAX.

Fig. 10. Diagram of rays which arrive and are reflected by the designed mirrors.

Fig. 11. Front view of the designed mirror, simulated with ZEMAX.

The results obtained of the images generated of the point source at infinity by each mirror, and their corresponding irradiance distributions, are shown in Figs. 12 to 15. These figures show the respective results of the design using spherical, parabolic, and elliptical rings, and with conic constant calculated with GA. The image sizes shown in each one of these figures agree with those reported in Table 1 from the optimization stage.

Once the results obtained from the optimization stage have been validated with ZEMAX, the final stage in the simulation process, in which the sun is considered as object, is to replace the point source with the sun source in ZEMAX.

Fig. 12. a) Image of the point source, placed at infinity, generated by the mirror designed with spherical surface rings, and b) its corresponding irradiance distribution graph.

Fig. 13. a) Image of point source, placed at infinity, generated by the mirror designed with parabolic surface rings, and b) its corresponding irradiance distribution graph.

Fig. 14. a) Image of the point source placed at infinity, generated by the mirror designed from elliptical surface rings (conic constant equal to -0.5), and b) its corresponding irradiance graph.

Fig. 15. a) Image of the point source, placed at infinity, generated by the mirror designed with rings having a conic constant calculated with GA equal to a -1.6279, and b) its corresponding irradiance distribution graph.

3.2 Simulations done using the sun source as object

To simulate sun images generated by the designed mirrors, the sun source was generated in a DLL file by means of the following equation

$$B(\theta) = B_d \left[1 - (0.5051\theta / \alpha)^2 - (0.9499\theta / \alpha)^8 \right], \quad (4)$$

where $B_d = 13.639 \times 10^6 \text{ W/m}^2 \text{ stereorad}$ and $\alpha = 4.653 \text{ rad}$.

While the aureola region was adjusted by the following equation

$$B(\theta) = B_a (\theta / \alpha)^{-2}, \quad (5)$$

where $B_a = 72,200 \text{ W/m}^2 \text{ stereorad}$.

Fig. 16 shows the statement of the sun source in the ZEMAX program, while Fig. 17 shows the image of the sun before arriving at the mirror, at a distance of 150 mm from the vertex.

Non-Sequential Component Editor									
Object Type	Comment	Ref Object	Inside OC	X Position	Y Position	Z Position	Tilt About X	Tilt About Y	Tilt About Z
1	Source DLL	FUENTE 01.DLL	0	0.000000	0.000000	-1000.000000	0.000000	0.000000	0.000000

Non-Sequential Component Editor									
Object Type	Tilt About X	Tilt About Y	Tilt About Z	Material	# Layout Rays	# Analysis Rays	Power (Watts)	Wavelengths	
1	Source DLL	0.000000	0.000000	-	1000	20000000	1.000000	0	

Non-Sequential Component Editor									
Object Type	Color #	B	Par 7 (unused)	Par 8 (unused)	Par 9 (unused)	Par 10 (unused)	Par 11 (unused)	Par 12 (unused)	Par 13 (unused)
1	Source DLL	0	800.000000						

Fig. 16. Statement of the sun source in the ZEMAX program.

(a)

(b)

Fig. 17. a) Simulation of the sun source before arriving at the mirror, and together with b) its respective irradiance distribution.

Figs. 18 to 21 show the simulations of sun images with their respective distributions of irradiance generated with the mirrors designed with spherical, parabolic, elliptical rings, and rings with conic constant calculated with GA, respectively. Each one of these images was simulated with the ZEMAX program at a distance of -1973 mm. According to the FWHM criterion, the sizes of sun images generated by each mirror are shown in Table 2.

Fig. 18. a) Image of the sun source generated by the mirror designed with spherical surface rings, and b) their corresponding graph of irradiance distribution.

Fig. 19. a) Image of the sun source generated by the mirror designed with parabolic surface rings, and b) their corresponding graph of irradiance distribution.

Fig. 20. a) Image of the sun source generated by the mirror designed with elliptical surface rings, with a conic constant of -0.5 and b), its corresponding graph of irradiance distribution.

Fig. 21. a) Image of the sun source generated by the mirror designed from rings with a conic constant equal to -1.6279 calculated with GA, and b) its corresponding graph of irradiance distribution.

Mirror designed with	Conic constant	Size of sun image (mm)
Spherical rings	0	16.97
Parabolic rings	-1	16.75
Elliptical rings	-0.5	16.89
Rings with a conic constant calculated with the GA	-1.6279	16.97

Table 2. Results of sun image sizes generated by the designed mirrors using the FWHM criterion.

As can be seen in Table 2, the sun image sizes obtained correspond to the angular sizes obtained from the images of the point source (see Table 1), that is, the biggest angular sizes correspond to the mirrors with rings whose conic constant was 0 and -1.6279. These very same mirrors are the ones that generate the biggest sun images, whereas the smallest images are generated with the mirror designed with elliptical surface rings with a conic constant of -0.5. Furthermore, the sun image sizes agree with the image size reported from using a mirror designed from concentric spherical rings (González-García, et al., 2009).

4. Conclusions

From the design of four mirrors which reduce by one order of magnitude the angular size of the image of a point source placed at infinity compared to an image generated by a spherical mirror, we could generalise the optical design method that uses the concept of concentric spherical rings for designing energy concentrators. The generalization of the method consisted in using concentric rings with conic surfaces in the optimization stage, considering two cases: 1) a constant value of the conic constant, and 2) the conic constant as one more variable to be optimized. The mirror designs could thereby remain in function of the value of the conic constant, as well as the paraxial curvature radii of the rings. The four mirrors

designed were simulated with the commercial optic design program ZEMAX, considering the sun as object. The images of the sun were compared to the images of the point source placed at infinity, and this revealed that the sizes of the images of the sun are related to the angular sizes of the images of the point source: the mirror design which generates the smallest angular size is the mirror which generates the smallest sun image, while the mirror which generates the biggest angular size is the mirror which generates the biggest sun image.

Finally, the results obtained show that it is possible to design mirrors, solar energy concentrators, from the concept of concentric rings with conic surfaces, thereby generating an alternative method of optical design for this type of mirrors. This type of method can also be applied in the design of lens concentrators.

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